

# Leakage and Guidance Properties of Unbalanced Insulated NRD-Guide for Co-Layered Integrated Circuits

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**Abstract** — Leakage and guidance characteristics of unbalanced insulated NRD-guide were studied by means of a mode-matching technique. Leakage suppressing condition and single mode operating condition are investigated for practical applications and the relations between geometrical parameters of the structure and the guided wave as well as leakage properties were obtained. Extensive results and useful guidelines were provided for practical application of this guided-wave structure in co-layered integration circuits.

## I. INTRODUCTION

Co-layered hybrid integration techniques based on NRD-guide and planar circuits become attractive for use in the design of millimeter-wave integrated circuits [1]. In this co-layered topology, the planar circuits are in direct physical contact with the NRD-guide, thus yielding a strong electromagnetic coupling between the two dissimilar structures. Very compact transitions can be designed with broadband features. However, leakage may also manifest in this structure because of potentially asymmetrical dielectric substrates. Therefore, how to suppress the leakage is critical to practical applications of this hybrid integrated structure.

This co-layered hybrid integration structure may actually form an insulated NRD-guide proposed by T.Yoneyama et al. [2]. In [2], propagation properties of the insulated NRD-guide were studied by means of EDC approach, but the phenomenon of leakage was not discussed as it was basically used for low loss guided-wave applications without considering the hybrid scheme of planar and NRD-guide circuits. Tang et al. [3] have analyzed characteristics related to the leakage of this structure and presented some pertinent physical effects such as leakage and resonance. However, there are

missing information in connection with the impact of leakage on the bandwidth of single operating mode. In this paper, we emphasize on investigation of the leakage condition by means of a mode-matching technique, therefore providing useful guidelines for deploying this co-layered hybrid platform in various millimeter-wave integrated circuits design.

## II. ANALYSIS AND NUMERICAL RESULTS

To begin with, we consider this co-layered structure as an unbalanced insulated NRD-guide. Fig. 1 shows the cross section of this guided-wave structure. According to the symmetry in x-direction, we can put one perfect electrical plane at  $x=0$  and therefore simplify our following analysis. By applying a mode-matching approach, we can readily obtain the propagation properties of this unbalanced or generalized insulated NRD-guide.

### A. Non-radiative Condition

From Fig. 1, we can see that the region outside the dielectric strip can be considered as a multilayered dielectric waveguide sandwiched with two metal plates. Therefore the non-radiative condition for unbalanced insulated NRD waveguide is just the cut-off condition for modes guided by layered slab dielectric waveguide outside the dielectric strip line.

This kind of layered slab dielectric waveguide has been thoroughly studied in [5]. The modal cut-off feature is shown in Fig. 2. From this figure we can find that the non-radiative condition for the unbalanced insulated NRD-guide is almost the same as that for the standard NRD waveguide without considering the lowest mode  $TM_1$ , i.e.

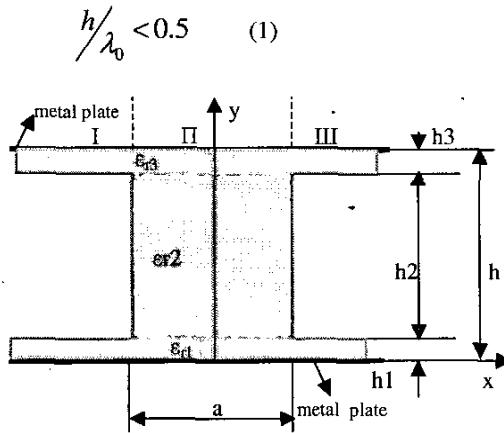


Fig. 1 Cross section of unbalanced insulated NRD-guide.

### B. Condition for Leakage

Wave propagation properties, including leakage, of the standard NRD guide has been extensively analyzed in [4] and the results illustrated that no leakage effects are present that could affect the behavior of NRD-guide components. When the dielectric strip line is sandwiched between substrates as shown in Fig. 1, the above conclusion obtained in [4] is no longer valid. Tang et al. have studied the leakage in this structure [3], but they failed to give the general condition related to leakage.

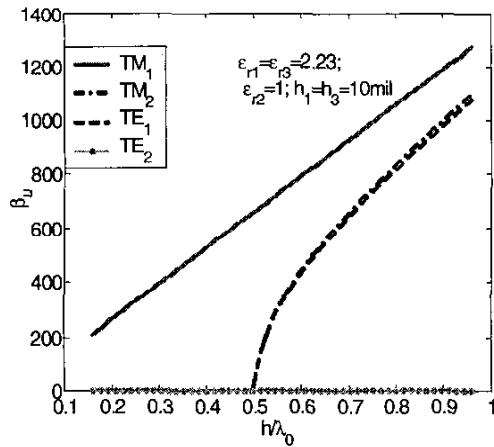


Fig. 2 Cutoff characteristics in layered slab guide ( $\beta_u$  is propagation constant).

For this unbalanced insulated NRD-guide, there are neither exact LSM nor LSE modes but hybrid types. The field distributions of modes are similar to those of the

pure LSM or LSE modes. We call such modes in this dielectric waveguide quasi-LSM mode or quasi-LSE modes. The working mode is quasi-LSM<sub>01</sub> mode.

Fig. 3 illustrates modal dispersion curve versus frequency. The working mode can be considered as a consequence by scattering when the lowest TE mode in the core dielectric strip is incident at an angle on the side of the dielectric strip. Because of TE-TM coupling at the dielectric interface, all kinds of TE and TM modes will be excited in the slab region III and I (see Fig. 1). The lowest mode in the slab waveguide is TM<sub>1</sub> mode. Since higher-order TM and TE modes are under cut-off condition (see Fig. 2), the mode that may carry energy away from the dielectric core strip and therefore result in leakage, may only be TM<sub>1</sub> mode in the layered slab waveguide. Suppose that  $\beta_u$  is the propagation constant of this TM mode, and  $\beta_z$  is for quasi-LSM<sub>01</sub> mode. Then the condition for leakage is

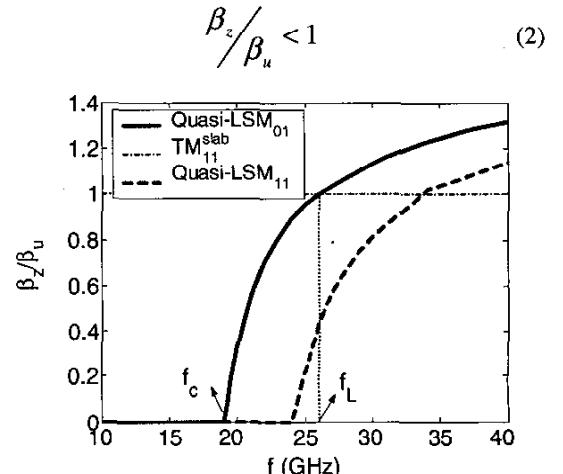


Fig. 3 Propagation characteristics of unbalanced insulated NRD-guide.

Equation (2) means that if we let  $\beta_z > \beta_u$ , we can suppress the leakage. It should be noted that the above condition is a general rule for leakage and this condition is different from that for the leakage cancellation:  $(k_x a)_{in} = 2\pi$ , under which the leakage is cancelled because of the resonance effects as discussed in [3]. For the purpose of practical design, we should adequately choose the geometrical parameters of waveguide to dissatisfy the condition set by (2).

From Fig. 3 we can find that as frequency increases, the mode propagation presents three distinct regions: "classical" cutoff phase, leakage, and bounded states. This is quite different from that in the standard NRD

waveguide. When  $f$  is less than  $f_C$ , the mode is cutoff, and while  $f$  is between  $f_C$  and  $f_L$ , the mode is leaky. Only when  $f$  is higher than  $f_L$ , the mode is bounded as in a standard NRD waveguide. We should call  $f_L$  the characteristic frequency at which  $\beta_z/\beta_u = 1$ .

Fig.4 presents influence of dielectric constant of the core dielectric strip on  $f_L$  for the quasi- $LSM_{01}$  mode. When only  $\epsilon_{r2}$  increases,  $\beta_z$  will increase at the same frequency point, but  $\beta_u$  does not change. Therefore we can find that with  $\epsilon_{r2}$  increasing,  $f_L$  shifts to lower frequency and therefore the bandwidth in the absence of leakage increases.

Fig.5 illustrates the dependence of  $f_L$  on width "a" of the core dielectric strip line. Suppose that the effective dielectric constant in core strip region II (see Fig. 1) is  $\epsilon_{e1}$ , then  $\beta_z = (\epsilon_{e1}k_0^2 - k_x^2)^{1/2}$ , in which  $k_x$  is the wave number in x-direction in the core dielectric region. When "a" is changed while keeping other parameters constant,  $k_x$  will vary with "a", but  $k_x$  must satisfy the eigenvalue equation in x-direction. So  $\beta_z$  will be different at the same frequency with different "a". Meanwhile,  $\beta_u$  is constant, so  $f_L$  at which  $\beta_z = \beta_u$  will vary with "a". There is an optimum width "a" at which we can get minimum  $f_L$ .

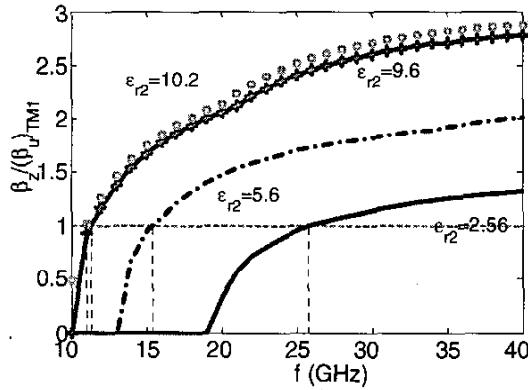


Fig. 4 Effect of dielectric constant  $\epsilon_{r2}$  on  $f_L$  for quasi- $LSM_{01}$  mode with  $h_1=h_3=10\text{mil}$ ,  $h=4.8\text{mm}$ ,  $a=4.3\text{mm}$ , and  $\epsilon_{r1}=\epsilon_{r3}=2.23$ .

Fig.6 displays the effect of asymmetry in y-direction on the characteristic frequency  $f_L$ . We use  $\Delta h=h_3-h_1$  to express the degree of asymmetry. For symmetric substrates,  $\Delta h=0$ . We keep the space  $h$  between the two metal plates constant.

Suppose that the effective dielectric constant in region III and I is  $\epsilon_{e2}$ . When  $\Delta h$  increases,  $\epsilon_{e2}$  will increase and therefore  $\beta_u$  will increase at the same frequency. As we can find from Fig. 6 that with increasing  $\Delta h$ , the

characteristics  $f_L$  shift towards to higher frequency and bandwidth without leakage will decrease.

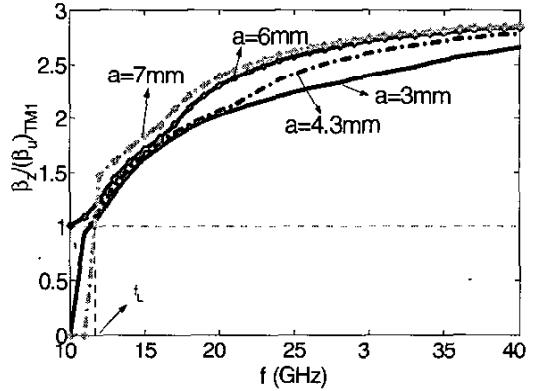


Fig. 5 Effect of width "a" of the core dielectric strip line on  $f_L$  of quasi- $LSM_{01}$  mode with  $h_1=h_3=10\text{mil}$ ,  $h=4.8\text{mm}$ ,  $\epsilon_{r1}=\epsilon_{r3}=2.23$ , and  $\epsilon_{r2}=9.6$

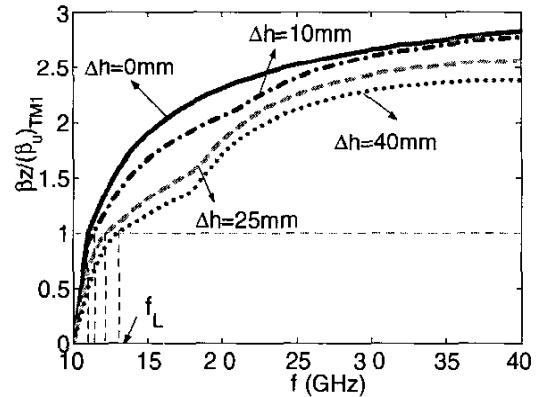


Fig. 6 Effect of asymmetry degree  $\Delta h=(h_3-h_1)$  on  $f_L$  for quasi- $LSM_{01}$  mode with  $h_1=10\text{mil}$ ,  $h=4.8\text{mm}$ ,  $a=4.3\text{mm}$ , and  $\epsilon_{r1}=\epsilon_{r3}=2.23$ ,  $\epsilon_{r2}=9.6$ .

### C. Single Mode Bandwidth Without Leakage

It is quite different from the standard NRD waveguide where the operating mode is not leaky. For the operating mode in unbalanced insulated NRD waveguide, leakage may be well present, as we have discussed in the above section. Therefore, as far as the monomode conditions are concerned, we must look into the conditions in the absence of leakage. For the single mode operation without leakage, the following requirements must be satisfied

$$\begin{cases} \lambda_0/2, \lambda_{g0}/2 > h > \lambda_{g1}/2 \\ \beta_z/\beta_u > 1 \end{cases} \quad (3)$$

in which  $\lambda_{g0}$ ,  $\lambda_{g1}$  are the guided wavelengths of quasi- $LSM_{01}$  and quasi- $LSM_{11}$  modes.

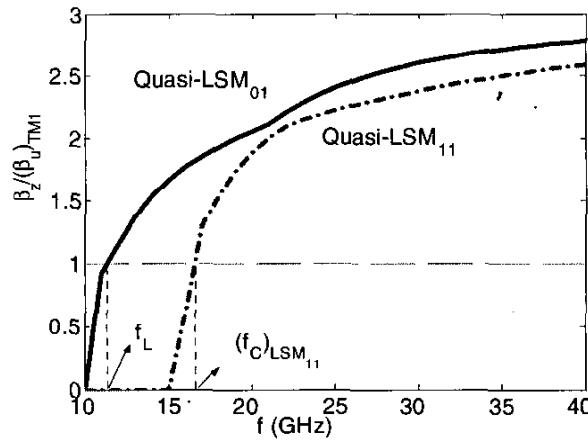


Fig. 7 Frequency range of single mode operation without leakage with parameters  $h_1=h_3=10\text{ mil}$ ,  $h=4.8\text{ mm}$ ,  $a=4.3\text{ mm}$ , and  $\epsilon_r=2.23$ ,  $\epsilon_r=9.6$

Fig. 7 shows the frequency range with the single mode operation. From this figure we can see that the single mode bandwidth without leakage is  $B=(f_c)_{LSM_{11}}-f_L$ . Because of the leakage, the bandwidth is smaller than that in the standard NRD-guide, where the bandwidth is just  $(f_c)_{LSM_{11}}- (f_c)_{LSM_{01}}$ . In the case of  $(f_c)_{LSM_{11}} < (f_L)_{LSM_{01}}$ , there will not exist a single mode operation frequency range without leakage.

Fig. 3 shows this scenario, where the cutoff frequency of  $LSM_{11}$  mode is less than the characteristic frequency  $f_L$

of the quasi- $LSM_{01}$  mode. To increase the bandwidth  $B$ , we should try to decrease the characteristic frequency  $f_L$  to  $(f_c)_{LSM_{01}}$ . From Fig.4 we know that we can get a smaller  $f_L$  by using the core dielectric strip line with higher permittivity.

### III. CONCLUSION

We have presented general properties of wave guidance and leakage of the insulated NRD-guide. We can conclude that the unbalanced insulated NRD-guide preserves most properties of the standard NRD-guide under certain conditions. The effect of leakage will reduce the effective bandwidth of single mode operation. This guided-wave structure can be applied in the design platform for low-loss and low-cost co-layered hybrid integrated microwave and millimeter wave circuits.

### REFERENCES

- [1] J. Tang, K. Wu, "Co-layered integration and interconnect of planar circuits and non-radiative dielectric (NRD) waveguide," *IEEE Trans. Microwave Theory and Tech.*, vol. MTT-48, no. 4, pp519-524, April 2000.
- [2] T. Yoneyama, S. Fujita, and S. Nishida, "Insulated Nonradiative Dielectric Waveguide for Millimeter-Wave Integrated Circuits," *IEEE Trans. Microwave Theory and Tech.*, vol. MTT-31, no. 12, pp1002-1008, December 1983.
- [3] J. Tang, X.-Y. Zeng, S.-J. Xu, K. Wu, "Low-loss millimeter-wave propagation characteristics of NRD-guide surface-mounted on planar substrate for hybrid integrated circuit," *2000 IEEE MTT-S Int. Microwave Symp. Dig.*, pp. 1679-1682, June 2000.
- [4] C. Di Nallo, F. Frezza, A. Galli, G. Gerosa, P. Lamariello, and A. A. Oliner, "Properties of NRD-Guide and H-Guide Higher-Order Modes: Physical and Nonphysical Ranges," *IEEE Trans. Microwave Theory and Tech.*, vol. MTT-42, no. 12, pp2429-2434, December 1994.
- [5] R. E. Collin, *Field Theory of Guided Waves*, New York : IEEE Press, 1991.